

NOMENCLATURE

b	Width of roughness elements, helical channel, lobes of twisted tubes, space between tubes within a bundle, m
$c_f = 2\tau_w/\rho u_\infty^2$	Friction coefficient
c_p	Specific heat, J/kg · K
D	Diameter of the curvature of a coiled passage, m
d_0	Diameter of the cylinder, of the zero shear stress surface, describing a coiled tube, m
d_1, d_2	Diameters of washed surfaces of tubes comprising an annular or helical channel, m
d_e	Equivalent diameter of channel, m
E	Voltage across the anemometer wires, V
F	Net cross-sectional area, heating-wall surface, m ²
G	Working-fluid flow rate, kg/sec; coefficient
$G(k^+), G_1(k^+)$	Thermal functions of roughness
$H = \delta^*/\delta^{**}$	Shape factor
h	Height of helical passage, m
I	Current, A
k	Height of roughness projections, m
$k^+ = ku_*/\nu$	Dimensionless height of roughness projections at temperature T_f
l	Mixing length, length of channel, m
p	Pressure, Pa
Δp	Pressure differential, Pa
Q	Heat flux, W
q	Heat flux density, W/m ²
$R(k^+), R_1(k^+)$	Hydrodynamic functions of roughness
r	Tube radius, current radius, m
r_0	Radius of cylinder, of zero shear stress surface, m
$r_0^+ = r_0 u_*/\nu$	Dimensionless radius
s	Spacing between roughness elements, pitch of helical channel, of twisted tubes, m
s_1	Pitch of tubes within a bundle, m
T	Temperature, K

U	Potential drop, V
u, v, w	Velocity components, m/sec
u', v', w'	Velocity fluctuations, m/sec
u_0	Bulk velocity, m/sec
u_∞	Free-stream velocity, m/sec
u_r, u_τ	Radial and tangential velocity components, m/sec
$u_* = \sqrt{\tau_w/\rho}$	Friction velocity, m/sec
$u^+ = u/u_*$	Dimensionless velocity
\mathbf{V}	Total-velocity vector, m/sec
x, y, z	Cartesian coordinates
x	Length, distance from start of heating, m
x_0	Virtual start of turbulent boundary layer, m
y	Current distance along the radius, calculated from the surface of tubes or cylinder, m
$y^+ = yu_*/\nu$	Dimensionless distance
$y_R = r_0 \ln(r/r_0)$	Coordinate of axisymmetric boundary layer, m
$y_R^+ = r_0^+ \ln(r/r_0)$	Dimensionless coordinate
α	Heat-transfer coefficient, W/m ² · K; angle, radius
δ	Thickness of boundary layer, of wall, m
δ^*	Displacement thickness, m
δ^{**}	Momentum thickness, m
ε_q	Eddy thermal diffusivity, m ² /sec
ε_τ	Eddy viscosity, m ² /sec
η	Efficiency
$\vartheta = T_w - T$	Temperature differential, K
$\vartheta_* = q_w/\rho c_p u_*$	Characteristic temperature, K
$\vartheta^+ = \vartheta/\vartheta_*$	Dimensionless temperature
κ	Universal constant
$\Lambda = l/\delta_x$	Normalized mixing length
λ	Thermal conductivity, W/m · K
μ	Dynamic viscosity, N · sec/m ²
ν	Kinematic viscosity, m ² /sec
ξ	Hydraulic drag coefficient
Π	Channel perimeter, m
ρ	Density, kg/m ³
τ	Shear stress, N/m ²
φ	Angle, degrees
$\Psi = T_w/T_f$	Temperature factor
$\text{Fr}_M = s^2/d_0 d_e$	Modified Froude number

$Nu = \alpha d_e / \lambda$, $Nu_x = \alpha x / \lambda$	Nusselt numbers at pertinent reference parameters
$Pr = \mu c_p / \lambda$	Prandtl number
$Pr_T = \varepsilon_\tau / \varepsilon_q$	Turbulent Prandtl number
$Re = u_0 d_e / \nu$	Reynolds numbers at pertinent reference parameters
$Re_{r_0} = u_\infty r_0 / \nu$	
$Re_x = u_\infty x / \nu$	
$Re_{\delta^*} = u_\infty \delta^* / \nu$	
$St = \alpha / \rho c_p u_\infty$ $= Nu / Re Pr$	Stanton number at pertinent reference parameters
$Tu_\infty = \sqrt{u'^2} / u_\infty$	Turbulence intensity

Subscripts

0	At the plate, for a smooth surface, for the channel as a whole
1	Inner tube, zone of annular channel
2	Outer tube, zone of annular channel
∞	In the free stream, in the stabilized heat-transfer region
f	In the flow
in	At the inlet
out	At the exit
s	For sand roughness
t	In the tube
tr	Upon transition from partial to complete manifestation of roughness
w	At the wall
$\Psi = 1$	At constant physical properties
$(\bar{})$	Averaging

Other symbols are defined in the text.