

NOMENCLATURE

- b – channel width, m;
 $c_f = 2\tau_w/\rho u^2$ – skin friction coefficient;
 c_p – specific heat, J/(kg·K);
 D – curvature diameter, m;
 d – diameter, m;
 d_1, d_2 – wetted surface diameters of the tubes of annular or helical channel, m;
 d_e – equivalent diameter of the channels, m;
 $E = (\overline{u'^2} + \overline{v'^2} + \overline{w'^2})/2$ – turbulence energy, m²/s²;
 F – flow section area, m;
 g – acceleration due to gravity, m/s²;
 h – channel height, m; enthalpy, J/kg;
 $h_* = q_w/\rho u_*$ – characteristic enthalpy, J/kg;
 $K = (v/u^2)(du/dy)$ – acceleration parameter;
 $K = Gr_A/Re^2$ – natural convection (bouyancy) parameter;
 l – channel length along the axial line; turbulence scale, m;
 $l_+ = lu_*/\nu$ – dimensionless turbulence scale;
 l_t – thermal turbulence scale, m;
 P, p – pressure, Pa;
 q – heat flux density, W/m²;
 $q^+ = q_w/h\bar{u}\rho$ – heat flux parameter;
 R – curvature radius, m;
 r – current radius, m;
 r_o – tube radius, m;
 s – twist pitch of the channel, m;
 T – temperature, K;
 $T_* = q_w/\rho c_p u_*$ – characteristic temperature, K;
 $T^+ = (T_w - T)/T_*$ – dimensionless temperature;
 u – flow velocity, m/s;

- $u_* = \sqrt{\tau_w/\rho}$ – friction velocity, m/s;
 $u^+ = u/u_*$ – dimensionless velocity;
 u, v, w – velocity components, m/s;
 $\overline{u'v'_+} = -\overline{u'T'_+}/u_*^2$ – dimensionless turbulent shearing stresses;
 $\overline{u'T'_+} = \overline{u'T'_+}/u_*T_*$ – dimensionless turbulent axial heat transfer;
 $\overline{v'^2_+} = \overline{v'^2}/u_*^2$ – dimensionless intensity of radial velocity oscillations;
 $v'T'_+ = -v'T'_+/u_*T_*$ – dimensionless turbulent radial heat transfer;
 x – longitudinal coordinate, distance from the heating origin, m;
 $x_+ = xu_*/\nu$ – dimensionless longitudinal coordinate;
 y – transverse coordinate, m;
 $y^+ = yu_*/\nu$ – dimensionless transverse coordinate;
 α – heat transfer coefficient, W/(m²·K);
 $\beta = -1/\rho(\partial\rho/\partial T)_p$ – volumetric expansion coefficient, 1/K;
 Δ – maximal relative error;
 δ – boundary layer thickness, wall thickness, m;
 relative rms error;
 $\delta_{i,\alpha}$ – Kronecker delta;
 γ – intermittence coefficient;
 $\varepsilon = E^{3/2}/l$ – dissipation function;
 ε_t – thermal dissipation function;
 $\varepsilon_\tau = \overline{-u'v'}/(du/dy)$ – turbulent viscosity, m²/s;
 $\varepsilon_q = \overline{-v'T'}/(dT/dy)$ – eddy diffusivity, m²/s;
 θ – angle of curvature, deg;
 κ – universal constant;
 λ – thermal conductivity, W/(m·K);
 μ – dynamic viscosity, Pa·s;
 ν – kinematic viscosity, m²/s;
 ξ – friction factor;
 Π – wetted perimeter of the channel, m;
 ρ – density, kg/m³;
 τ – shear stress, N/m²;
 φ – angle, °, deg;

$$\psi = T_w / T_f \quad - \text{ temperature factor;}$$

$$\text{De} = \text{Re} \sqrt{d/D} \quad - \text{ Dean number;}$$

$$\text{Gr}_q = g\beta q_w d^4 \rho^2 / \lambda \mu^2 \quad - \text{ Grashof number defined by the heat flux specified on the surface;}$$

$$\text{Gr}_A = g\beta d^4 \left(\frac{dT_f}{dx} \right) \frac{1}{16\nu^2} \quad - \text{ Grashof number defined by the longitudinal gradient of the bulk temperature of the liquid;}$$

or
$$\text{Gr}_A = \frac{\text{Gr}_q}{4\text{RePr}}$$

$$\text{Nu} = \alpha d_e / \lambda \quad - \text{ Nusselt number;}$$

$$\text{Pr} = \mu c_p / \lambda \quad - \text{ Prandtl number;}$$

$$\text{Pr}_t = \varepsilon_\tau / \varepsilon_q \quad - \text{ turbulent Prandtl number;}$$

$$\text{Re} = \bar{u} d_e / \nu \quad - \text{ Reynolds number;}$$

$$\text{St} = \text{Nu} / \text{RePr} \quad - \text{ Stanton number.}$$

Subscripts:

- o – refers to a straight channel;
- 1 – inner tube;
- 2 – outer tube;
- ∞ – in the external flow, in the stabilized flow region;
- cr – laminar-turbulent flow transition;
- cr1 – beginning of transition;
- cr2 – end of transition;
- f – in the flow;
- in – at the inlet;
- L – laminar;
- T – straight tube, turbulent;
- w – at the wall;
- $\psi = 1$ – at constant physical properties;
- ($\bar{\quad}$) – averaging;
- (\prime) – oscillating component.

The remaining symbols are defined in the text.